

Trigonometric Limits. No Graphing Calculator is allowed for these problems. Also, do not use L'Hôpital's Rule.

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Evaluate the limits algebraically.

1. 
$$\lim_{x \rightarrow 0} \frac{\sin 3x}{x}$$

2. 
$$\lim_{x \rightarrow 0} \frac{3x}{\sin 5x}$$

3. 
$$\lim_{x \rightarrow 0} \frac{\sin(x^2)}{x}$$

4. 
$$\lim_{x \rightarrow 0} \frac{\sin x}{x^2}$$

5. 
$$\lim_{x \rightarrow 0} \frac{\sin^2 3x}{5x^2}$$

6. 
$$\lim_{x \rightarrow 0} \frac{2x}{\tan 3x}$$

7. 
$$\lim_{x \rightarrow 0} (x \csc x)$$

$$8. \quad \lim_{x \rightarrow 0} \frac{x^2}{1 - \cos x}$$

[ Hint: multiply the top and bottom by  $(1 + \cos x)$  . ]

$$9. \quad \lim_{x \rightarrow 0} \frac{1 - \sec^2 2x}{x^2}$$

$$10. \quad \lim_{x \rightarrow 0} \frac{2x^2 + x}{\sin x}$$

$$11. \lim_{x \rightarrow 0} \frac{\tan 3x}{2x^2 + 5x}$$

$$12. \lim_{x \rightarrow 0} \frac{\sin^2 x}{1 - \cos x}$$

$$13. \lim_{x \rightarrow 0} \frac{1}{2x \csc x}$$

14.  $\lim_{x \rightarrow \pi} \frac{\sin x}{x - \pi}$

[ Hint: Let  $A = x - \pi$  and use  
 $\sin(a + b) = (\sin a)(\cos b) + (\cos a)(\sin b)$  ]

15.  $\lim_{x \rightarrow \frac{\pi}{3}} \frac{\frac{1}{2} - \cos x}{x - \frac{\pi}{3}}$

[ Hint:  $\cos(a + b) = (\cos a)(\cos b) - (\sin a)(\sin b)$  ]

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**ANSWERS:**

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|--------|--------|---------|--------------------------|
| 1) 3   | 5) 9/5 | 9) -4   | 13) 1/2                  |
| 2) 3/5 | 6) 2/3 | 10) 1   | 14) -1                   |
| 3) 0   | 7) 1   | 11) 3/5 | 15) $\frac{\sqrt{3}}{2}$ |
| 4) DNE | 8) 2   | 12) 2   |                          |